Seminar at National Space Organization, Taiwan

Research Fields and Projects in Keldysh Institute for Applied Mathematics

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- What we are and who we are
- Collaboration with Taiwanese organizations
- Attitude control for microsatellite missions
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- Conclusion



Keldysh Institute for Applied Mathematics of Russian Academy of Sciences (KIAM)





Keldysh Institute for Applied Mathematics of Russian Academy of Sciences (KIAM)



KAM was established in 1953 to lead in the principal National Programs:

- exploration of space
- nuclear energy use
- development and application of numerical methods (for computers only growing)



Founder of the Institute



Academician Mstislav Keldysh was a Founder and a first Director in 1953-1978

In 60th he was officially named Principal Theoretician of the Soviet Cosmonautics but he is also known as a outstanding mathematician and mechanician



The famous 3K (Koroljev, Kurchatov, Keldysh)



From left to the right:

Sergey Koroljev – "the Chief Designer of the Soviet Cosmonautics"

Igor Curchatov – "the Father of the Soviet Nuclear Programm"

Mstislav Keldysh – "the Chief Theoretician of the Soviet Cosmonautics"



Main issues of KIAM's research activity

- Mathematical modeling and computer simulation to solve modern problems in science and technology
- Mathematical problems and theory of numerical methods development
- Fundamental and applied research in space flight mechanics
- Software development, parallel computing and multimedia application



Our scientists first applications in space

- Since First Artificial Satellite – Sputnik (4.10.1957) computing and multimedia application
- Through 1959 first taking picture of the Moon back side & first fly-by maneuver
- And another ...







Luna-3 exterior_{8/36}



Brief details about KIAM

- KIAM comprises 23 Departments and above 350 researcher including 3 Members and 4 Corr.-Memebrs of RAS, 60 Doctors of Sci. and 140 PhDs.
- KIAM's Ballistic Center is involved with the Mission Control Center (Korolyev City near Moscow) in a circus of mission control for manned and automatic SC.
- Main branches of research:
 - Fluid- and aeromechanics, nuclear processes,
 - numerical methods of computing and calculations,
 - theoretical mechanics, fundamental and applied celestial mechanics and control, robotics control,
 - IT and computer vision
- Educating Chairs of the Moscow State University, the Moscow Institute for Physics & Technology, the Bauman State Technological University located at KIAM



Our team





Areas of our competence

- space mission dynamics simulation,
- math models of dynamics development,
- attitude and orbital control algorithms synthesis,
- lab facilities implementation to validation campaign,
- small satellite strategy development,
- mission design

Branches of applications:

- single satellites for various applications within near-Earth missions including large communication and small-micro-nano-Cube satellites
- formations and constellations of satellites
- interplanetary missions to libration points and another planets 04.12.2017 Seminar at NSPO 11/36



KIAM's collaboration with Taiwan

Joint events (Workshops and Conferences held together):

- COSPAR Colloquium on Scientific Microsatellites. Microsatellite as Research Tools, National Cheng Kung University, December 1997, Tainan;
- Joint Taiwan Russian Symposium "Advanced Problems of Mechanics in Geology, External Geomonitoring and Wind Engineering", Ching Yun University, December, 2007, Jung-Li;
- 6th IAA International Workshop on Satellite Constellation and Formation Flying, November, 2010, National Space Organization (NSPO), Taipei;
- Remote Sensing Satellite Technology Workshop RSSTW2012, November, 2012, NSPO, Hsin-Chu

Projects:

- Dynamics and Control of Small Satellites in the Geomagnetic Field, Joint project # 07-01-92001 of the National Science Council of Taiwan and the Russian Foundation for Basic Research (2007-2010);
- Generic spacecraft dynamics simulation, Contract No.: NSPO-S-102089 (2013);
- Satellite multiple solar panel dynamics model development, Contract No.: NSPO-S-103132 (2014)



Mol between NSPO and KIAM (2010)



Dr. An-Ming Wu (Vice-Chair), Dr. Guey-Shin Chang (Chair), Prof. Mikhail Ovchinnikov, Dr. Andrey Baranov

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Partners' Small Sats with ACS developed by the team







The Russian microsatellite Chibis-M (launched in 2012). (credit SRI of RAS)



The Taiwanese satellite Formosat-7 (13), active active attitude control system, attitude control system, 250 kg(credit NSPO)



The American nanosatellite CXBN-2, active attitude control system, 2.5 kg (credit Morehead State University)



The Russian nanosat TNS-0 #2 (launched in 2017) passive magnetic attitude control system, 6 kg (credit JSC Russian Space Systems)



The German picosatellite (cubesat) BeeSat-3 (launched in 2013), passive attitude control system with hysteresis plate, 1 kg (credit TUB)



The Russian nanosatelliteSamSat-

QB50,aerodynamical attitude TNS-0 Nº1 (launched in 2005),magnetic attitude control control system with hysteresis passive magnetic attitude rods, 2 kg(creditSamara State control system, 4.5 kg Aerospace University) (credit JSC *Russian Space

Systems"



The first Russian nanosatellite The Russian nanosatellite TNS-1, active

system, self-rotation stabilization, 10 kg (credit JSC "Russian Space Systems")



The Russian AIS-Cubesat, active magnetic ACS, 3 kg (credit JSC Russian Space Systems)



The Italian microsatellite passive magnetic attitude control system, 12 kg (creditUniversity of Rome "La Sapienza")



The Pakistani microsatellite UniSat-4 (launched in 2004), BADR-B (launched in 2001). semiactive gravitational attitude control system, 70 kg gravity gradient attitude (credit SUPARCO)



The Russian nanosatellite REFLECTOR (launched in 2001), passive control system, 7 kg (credit Institute of Precision

Instrument Engineering)



The Swedish nanosatellite Munin, (launched in 2000), passive magnetic attitude control system, 6 kg (credit IRF)



The recent launch: TNS-0 №2 nanosatellite 17/08/2017





TNS-0 Nº2 nanosatellite angular motion



The estimated and measured unit magnetic vector

The estimated angular velocity



A current projects of our team

A few projects are under development in

- attitude control,
- orbital control,
- formation flying control,
- debris removal,
- interplanetary mission design



Satellite Attitude Control for Earth Remote Sensing and Communication





Complex trajectory tracking

Attitude stabilization of spacecraft with flexible elements



Mathematical model for Formasat-7 solar panel

To identify and control motion the mathematical model was developed and implemented

$$\mathbf{S}\begin{pmatrix}\dot{\boldsymbol{\omega}}_1\\\dot{\boldsymbol{\psi}}\end{pmatrix} = \begin{pmatrix}\mathbf{N}_1\\\mathbf{N}_2\end{pmatrix}$$



FORMOSAT 7

Here **S** is 8x8 matrix and for example is

$$\mathbf{N}_{1} = \sum_{i=1}^{4} \mathbf{M}_{i} - \mathbf{\omega}_{i} \times \mathbf{I}_{i} \mathbf{\omega}_{i} - \mathbf{I}_{2} \mathbf{f}_{2} - \mathbf{I}_{3} \mathbf{f}_{3} - \mathbf{I}_{4} \mathbf{f}_{4} - m_{1,2} \mathbf{d}_{1,2} \times \mathbf{j}_{1,2} - m_{1,3} \mathbf{d}_{1,3} \times \mathbf{j}_{1,3} - m_{1,4} \mathbf{d}_{1,4} \times \mathbf{j}_{1,4} - m_{2,3} \mathbf{d}_{2,3} \times \mathbf{j}_{2,3} - m_{2,4} \mathbf{d}_{2,4} \times \mathbf{j}_{2,4} - m_{3,4} \mathbf{d}_{3,4} \times \mathbf{j}_{3,4}$$



Satellite Formation Flying design

Two main directions of research:

- Direct and indirect optimization problems solution implementation (the control thrust can be directed wherever is needed)
- External forces implementation (aerodynamic resistance, Colomb interaction, mass exchange, solar pressure etc) and existed natural configurations seeking (subject of our interest)



Tetrahedron formation maintenance

Problem statement:

- Given four satellites on closed, possibly elliptical, orbits
- Need to obtain a reference orbit in order that the corresponding tetrahedron maintains over time
- Also provide a control algorithm for several satellites to neglect perturbations



image from NASA, MMS mission



Reference orbit for circular motion

 For reference orbit search we use linearized HCW model, closed orbits estimation

$$\begin{aligned} \ddot{x} - 2n\dot{y} - 3n^2x &= 0, \\ \ddot{y} + 2n\dot{x} &= 0, \\ \ddot{z} + n^2z &= 0 \end{aligned} \qquad \begin{aligned} x_i &= A_i \sin(nt + \varphi_i), \\ y_i &= C_i + 2A_i \cos(nt + \varphi_i) \\ z_i &= B_i \sin(nt + \psi_i) \end{aligned}$$



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• Introduce the *quality of the tetrahedron*

$$Q = 12 \frac{(3 | V |)^{2/3}}{r_{12}^2 + r_{13}^2 + r_{14}^2 + r_{23}^2 + r_{24}^2 + r_{34}^2} = 12 \frac{(3 | V |)^{2/3}}{L}$$

- Volume conservation is the conservation of the size
- Quality conservation is the conservation of the shape

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Fuelless FF Control Concepts

- Aerodynamic drag
- Electro-magnetic interaction
- Solar pressure
- Momentum exchange









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Swarm construction using aerodynamic force

 $\odot\,\text{Aerodynamic}$ force

$$\mathbf{f}_{i} = -\frac{1}{m}\rho V^{2}S\{(1-\varepsilon)(\mathbf{e}_{V},\mathbf{n}_{i})\mathbf{e}_{V} + 2\varepsilon(\mathbf{e}_{V},\mathbf{n}_{i})^{2}\mathbf{n}_{i} + (1-\varepsilon)\frac{\upsilon}{V}(\mathbf{e}_{V},\mathbf{n}_{i})\mathbf{n}_{i}\}^{*},$$

 $\mathbf{n} = (\cos\alpha\cos\beta; \sin\beta; \sin\alpha\cos\beta).$



Example of relative trajectories

Scheme of satellites launch



Single mass exchange control concept

- At command the single mass separates from the satellite
- The separated mass moves to the other satellite and impacts it absolutely inelastically
- After the whole mass transfer the resulting relative trajectory changes in adjustable way



the thrower before exchange
the separable mass
the thrower during exchange
the thrower after exchange



Space Debris in Low-Earth Orbits

- Kessler effect: a cascade of collisions of debris objects
- For low-Earth orbits, Kessler effect is likely to happen by mid-century





Sail-Assisted Deorbiting of LEO Nanosatellites

- Sail-assisted deorbiting is available even for the upper segment of LEO!
- The deorbit force is the SRP force rather than the drag force
- The required attitude regime can be established using the miniature CubeSat magnetorquers only
- Relative angular velocity damping

 $\boldsymbol{m}_1 = k_m \boldsymbol{\omega}_{rel} \times \boldsymbol{B}$

Differential spin rate damping

$$\boldsymbol{m}_{2} = k_{m} \left(\boldsymbol{\omega}_{\zeta} - \hat{\boldsymbol{\omega}}_{\zeta} \right) \boldsymbol{n} \times \boldsymbol{B}$$
$$\boldsymbol{m} = \begin{cases} \boldsymbol{m}_{1} + \boldsymbol{m}_{2}, \ \left| \boldsymbol{\omega}_{\zeta} - \hat{\boldsymbol{\omega}}_{\zeta} \right| \ge 10^{-4} \text{ rad/s} \\\\ \boldsymbol{m}_{1}, \ \left| \boldsymbol{\omega}_{\zeta} - \hat{\boldsymbol{\omega}}_{\zeta} \right| < 10^{-4} \text{ rad/s} \end{cases}$$







SRP-Augmented Disposal of GEO Satellites

The SRP force can be exploited at the final stage of transferring GEO satellites to a graveyard orbit





The initial phase of raising the orbit by 100-150 km with the use of thrusters is followed by the SRPaugmented phase (3–7 years)



Our competence in interplanetary mission design

- Libration point orbit (LPO) design
- Station-keeping and stability analysis of the LPOs
- Transfer trajectory design to the LPOs of the Earth-Moon or the Sun-Earth system
- Transfer trajectory design between the LPOs of the same or different three-body systems
- Low-thrust low-energy trajectory design suitable for small spacecraft in the Earth-Moon system



Equations of motion in the CR3BP

In the rotating frame $\ddot{x} - 2\dot{y} = U_x, \ \ddot{y} + 2\dot{x} = U_y, \ \ddot{z} = U_z$



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Planar and vertical Lyapunov orbits in the EM system



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Transfers between L1 and L2 halo orbits



Red line denotes unstable manifold around LP L1. Green line denotes stable manifold around LP L2

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Lab facilities in KIAM



Planar air bearing test bench COSMOS (COmplex for Satellites MOtion Simulation)

One-axis attitude control test bench

Magnetic field

Angular

determinatio

motion

imitator



Conclusion

Only a few examples have been given to represent wide area of our competence and directions of activity in dynamical models and control algorithms development for small satellites, laboratory testing and validation, flight data processing, mission design

Keldysh Institute of Applied Mathematics of the Russian Academy of Sciences:

- within competence open for collaboration
- ready to conduct studies for a customer
- ready to initiate joint projects in space area including Formation Flying and interplanetary missions



Thank you for your attention!

The full text publications in English are available at our web-site: http://keldysh.ru/microsatellites/eng/

