

# Low Energy Trajectories for the Moon-to-Earth Space Flight

V. V. Ivashkin

*Keldysh Institute of Applied Mathematics, Miusskaya Sq. 4, Moscow, 125047 Russia*

## Abstract

The Moon-to-Earth low energy trajectories of “detour” type are found and studied in frame of the Moon-Earth-Sun-particle system. These trajectories use a passive flight to the Earth from an initial elliptic selenocentric orbit with a high aposelenium and differ from usual ones of direct flight to the Earth using an initial hyperbolic selenocentric orbit. A numerical analysis and a qualitative theoretical one are performed for these trajectories. The Earth perturbation increases the particle selenocentric energy from a negative value first to zero and then to a positive one and therefore leads to a passive escape of the particle motion from the Moon attraction near the translunar libration point  $L_2$ . This results in the particle flight to a distance of about 1.5 million km from the Earth where the Sun gravitation decreases the particle orbit perigee distance to a small value that leads to the particle approach the Earth vicinity in about 100 days of the flight. A set of the Moon-to-Earth “detour” trajectories for the flight to the geocentric altitude of 50 km for the atmospheric reentry is defined by a numerical method. The start with a high thrust from both a low orbit of the Moon satellite and the Moon surface is considered. Characteristics of these trajectories are presented. They are compared with the usual trajectories of the direct flight. The “detour” Moon-to-Earth trajectories with initial elliptic orbit and gravitational escape from the Moon attraction are shown to result in essential economy of energy (about 150 m/s in  $\Delta V$ ) relative to the usual ones with initial hyperbolic orbit. A more exact control system of navigation and correction is required for the Moon-to-Earth “detour” flight of spacecraft.

**Key Words:** lunar trajectories, Moon-Earth flight, gravitational escape, gravitational perturbations, “detour” lunar flights

## 1. Introduction

Investigations of space trajectories for flights from the near-Moon vicinity to the Earth are important for both Celestial Mechanics and Astronautics. Usual trajectories (see, e.g., Egorov and Gusev 1980) for the Moon-to-Earth direct space flights within the Earth’s sphere of influence with respect to the Sun are well studied. In this case, perturbations caused by the Sun are small, and the model of the restricted three-body problem (Moon-Earth with a particle of negligible mass) is used in fact. Trajectories of this type were used for space flights from the Moon in both the USA project of the Apollo manned flight and the Soviet project for robotic capture of the lunar matter and its delivery to the Earth (see, e.g., Gatland 1982). These trajectories are characterized by small (several days) flight time and by the fact that the departure of the particle from the Moon occurs along a hyperbola. Recently (see, e.g., Belbruno and Miller 1993, Hiroshi Yamakawa et al 1993, Belló Mora et al 2000, Koon et al 2001, Ivashkin 2002, 2003, 2004a), a new class of trajectories with the Earth-to-Moon indirect detour space flight was discovered in the framework of the four-body system (Earth-Moon-Sun-particle). These trajectories use first the space flights towards the Sun (or away from the Sun) beyond the Earth’s sphere of influence, and only afterwards, space flights towards the Moon. These space flights seem to be similar to bielliptic ones proposed by Sternfeld

(1934, 1937, 1956). But they differ in dynamics. Here, the perigee distance rises due to the Sun gravitation. In addition, now the particle approaches the Moon along an elliptic trajectory, i.e., the capture by the Moon takes place. Thus, for the spacecraft capture to the lunar satellite orbit or for its landing onto the Moon, these detour space flights are more profitable than direct or bielliptic ones. An idea arises to employ this detour scheme for the Moon-to-Earth space flights (Hiroshi Yamakawa et al 1993, Ivashkin 2004b, 2004c). The present paper describes main results of numerical and analytical studies in the problem shown. A family of trajectories for passive space flight to the Earth from an elliptic orbit of a lunar satellite has been constructed, and characteristics of these trajectories are analyzed (Ivashkin 2004b, 2004c). In addition, the effects of gravitational perturbations resulted in the formation of these trajectories, particularly, in both the particle's gravitational escape from the lunar attraction and passive decreasing the perigee distance of the particle orbit (approximately from the value of the lunar orbit radius to almost zero), which makes possible the particle passive flights to the Earth, have been analyzed.

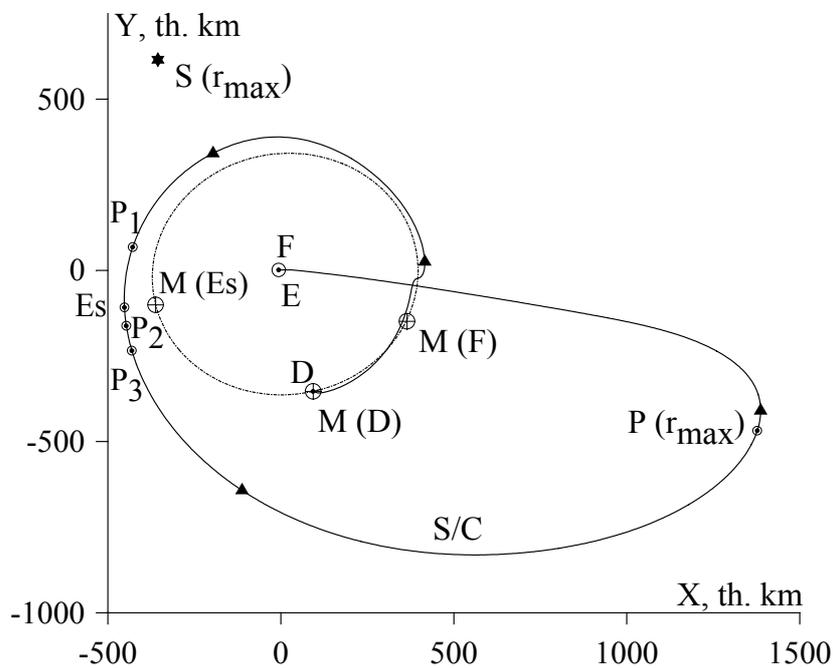


Figure 1. The XY geocentric view for the Moon-to-Earth trajectory of detour flight.

## 2. Moon-to-Earth detour trajectories

### 2.1 Algorithm of Calculations

As a result of the analysis and with taking into account the experience of the Earth-to-Moon trajectories studies (Ivashkin 2002, 2003, 2004a), a numerical algorithm has been developed that has allowed us to find a family of detour trajectories for space flights to the Earth from elliptic orbits of the lunar satellite. These trajectories correspond to the spacecraft start from both the Moon's surface and the low orbit of the lunar satellite for several positions of the Moon on its orbit. The spacecraft trajectories have been determined by integration using the method described in (Stepan'yants and L'vov 2000) of the equations for the particle motion. These equations are written in the Cartesian nonrotating geocentric-equatorial coordinate system OXYZ in the attraction field of

the Earth (with taking into account its main harmonic  $c_{20}$ ), the Moon, and the Sun with the high-precision determination of the Moon and Sun coordinates, which is based on the DE403 JPL ephemerides. The particle motion in the selenocentric coordinate system MXYZ is also determined.

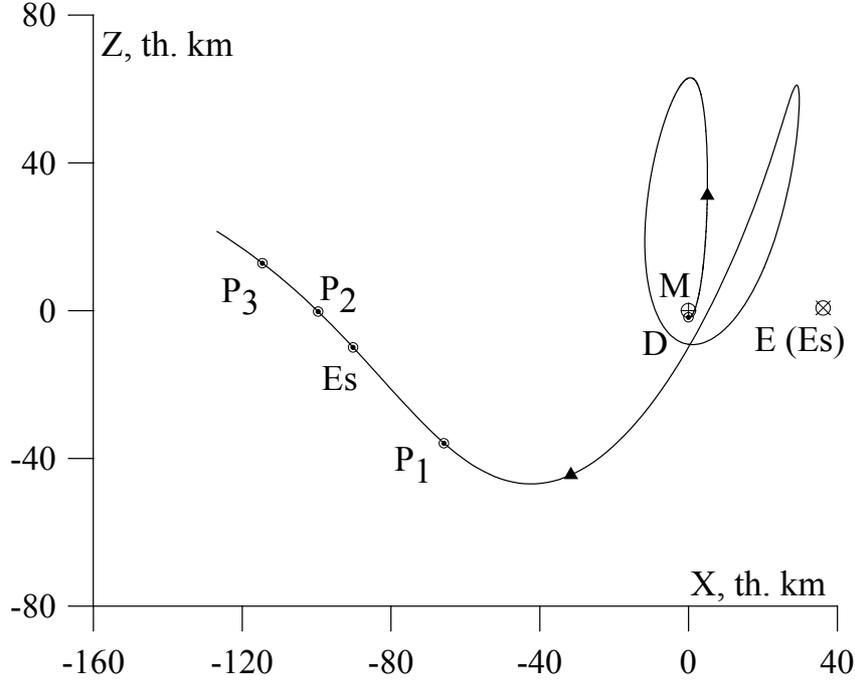


Figure 2. The XZ selenocentric view for the Moon-to-Earth trajectory of detour type at initial part of the flight.

## 2.2 Some Numerical Characteristics of the Moon-to-Earth Detour Flights

Characteristics of a typical detour trajectory are presented in Figures 1-3. The solid curve in Figure 1 presents geocentric motion of a spacecraft, and the dot-and-dash line shows the lunar orbit M. At the point D, the spacecraft flies away from the Moon on May 11, 2001 (for the position of the Moon near the apogee), from the perilune of an initial elliptic orbit with the perilune altitude  $H_{\pi 0} = 100$  km and semimajor axis  $a_0 = 38\,455$  km. This orbit is close to the final orbit of the Earth-to-Moon space flight, which was presented in (Ivashkin 2002, 2003, 2004a). All the following motion of the particle is passive (without taking into account possible corrections). Under the effect of the Earth's gravitation, evolution of the selenocentric orbit and an increase in the selenocentric energy

$$E_s = V^2 / 2 - \mu_M / \rho = -\mu_M / 2a_s \quad (1)$$

occur. In Eqn. 1  $V$  and  $\rho$  are the selenocentric velocity of the particle and its distance from the Moon, respectively,  $a_s$  is semimajor axis of the particle orbit, and  $\mu_M$  ( $\approx 4902 \text{ km}^3 \text{ s}^{-2}$ ) is the lunar gravitational parameter. At the point P1 in the space flight time  $\Delta t \approx 19$  days, the energy is  $E_s \approx -0.031 \text{ km}^3 \text{ s}^{-2}$ ,  $a_s \approx 79 \cdot 10^3 \text{ km}$ , and  $\rho \approx 76 \cdot 10^3 \text{ km}$ . At the point Es for  $\Delta t \approx 20.6$  days and  $\rho \approx 91.85 \cdot 10^3 \text{ km}$  in the region of the translunar libration point L2, there is the escape from the lunar

attraction, i.e.,  $E_s = 0$  here, and the orbit is parabolic with the zero velocity “at infinity”,  $V_\infty = 0$ . Further, the particle moves from the Moon along a hyperbola. At the point  $P_2$  for  $\Delta t \approx 21.1$  days and  $\rho \approx 101 \cdot 10^3$  km, the energy is  $E_s \approx 0.011 \text{ km}^2 \text{ s}^{-2}$ ,  $V_\infty = 0.15 \text{ km s}^{-1}$ . At the point  $P_3$  for  $\Delta t \approx 21.9$  days and  $\rho \approx 120.2 \cdot 10^3$  km, the energy becomes equal to  $E_s \approx 0.031 \text{ km}^2 \text{ s}^{-2}$ , and  $V_\infty = 0.25 \text{ km/s}$ . Then, the spacecraft flies away from both the lunar orbit and the Earth and reaches in  $\Delta t \approx 70$  days the maximal distance  $r_{max} \approx 1470 \cdot 10^3$  km from the Earth. At that moment, the point S ( $r_{max}$ ) determines the direction to the Sun. By the effect of the Sun gravitation, the perigee is gradually lowered, and for  $\Delta t \approx 113$  days at the point F, the spacecraft approaches the Earth E having the perigee’s osculating altitude  $H_\pi = 50$  km.

Figures 2 and 3 show the evolution of the spacecraft detour motion with respect to the Moon at the initial part of the space flight where there is the escape from the lunar attraction. Figure 2 gives selenocentric trajectory in the XZ plane. The point E (Es) determines the direction to the Earth at the moment of the escape from the lunar gravitational attraction. Figure 3 gives the selenocentric energy constant  $2E_s$  versus the time for the initial part D  $P_1$  Es  $P_2$   $P_3$  of the motion with escape from the lunar attraction. Here and below, on Figure 5, the time  $t$  is counted off from the Julian date 2451898.5, that is 20.12.2000.0.

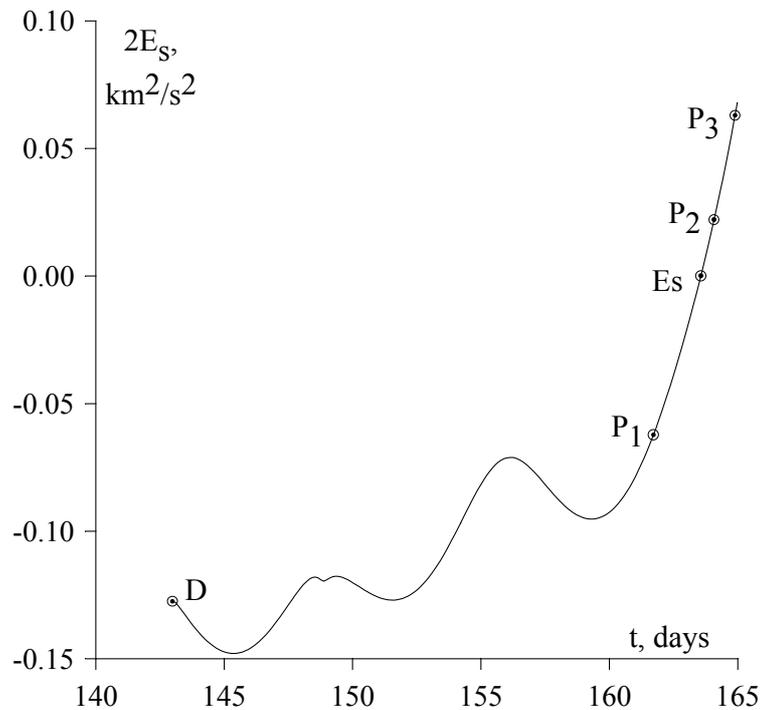


Figure 3. Selenocentric energy versus the time for initial part of the Moon-to-Earth detour flight with escape from the lunar attraction.

The initial (at the point D) velocity of spacecraft is  $V_0^+ \approx 2282 \text{ m s}^{-1}$ . For leaving a circular lunar-satellite orbit with altitude of 100 km and velocity  $V_0^- \approx 1633 \text{ m s}^{-1}$  using a velocity impulse (a high thrust), the velocity increment is  $\Delta V_0 \approx 649 \text{ m s}^{-1}$ . For the usual direct space flight scheme and the minimal departure energy,  $V_\infty \approx 0.8 \text{ km s}^{-1}$ , the flight time  $T \approx 5.5$  days, we have the initial velocity  $V_0^+$  of about  $2443 \text{ m s}^{-1}$ , the velocity impulse  $\Delta V_0$  of about  $810 \text{ m s}^{-1}$ , that is at  $dV_0 \approx 161 \text{ m/s}$  more than for the case of detour space flight.

For a case when spacecraft leaves the Moon surface, the detour trajectory (with  $a_0 = 38455$  km again) has approximately the same characteristics as for the indicated case of the start from the lunar satellite orbit. The decrease in the velocity increment is equal to about  $dV_0 \approx 156$  m/s in this case.

If initial semimajor axis  $a_0$  is less, the decreasing  $dV_0$  of the velocity impulse for the detour flight relative to the direct one is more. Figure 4 gives this decreasing  $dV_0$  versus the initial semimajor axis  $a_0$  of detour flight for two values of the velocity at “infinity”  $V_\infty = V_{inf}$  for direct flight:  $V_\infty = 0.8$  km/s (approximately, for optimal direct flight from the Moon apogee) and  $V_\infty = 0.9$  km/s (approximately, for optimal direct flight from the Moon perigee). The lines  $H_0 = 100$  km correspond to the spacecraft start from the satellite orbit perilune with altitude  $H_0 = 100$  km. The lines  $H_0 = 0$  correspond to the spacecraft start from the Moon surface. Possible values of the initial semimajor axis  $a_0$  for the detour flight are given below, in item 3.

**Remark.** Of course, these “detour” trajectories can be applied for the flight from a low-Moon orbit using an electric-jet engine with a low thrust, too.

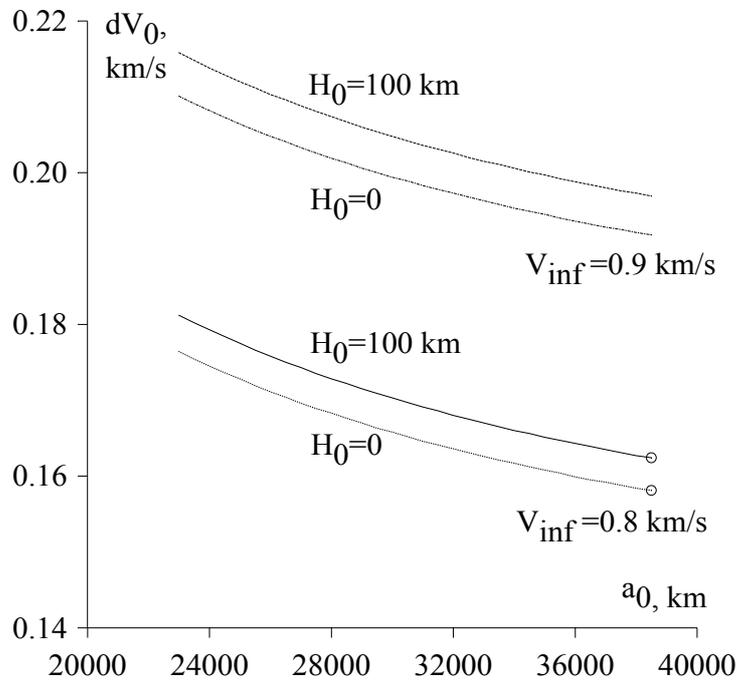


Figure 4. Decreasing of the velocity impulse for the Moon-Earth detour flight relative to the direct flight depending on the initial semimajor axis.

### 3. Earth’s gravity effect on the particle escape

We now qualitatively analyze the gravitational effects on the formation of the detour trajectory. First, we estimate an increase  $\Delta E_s = -E_{s0}$  of selenocentric energy (1) from the negative value  $E_{s0}$  for the initial elliptic orbit to the zero energy which can be caused by the Earth gravity during the particle selenocentric motion on the arc D Es from the initial state D to the escape point Es. On the base of the orbit evolution theory (Lidov 1961, 1962) and assuming that the particle’s selenocentric orbit eccentricity is  $e_s \approx 1$ , the mean energy is  $E_s \approx -\Delta E_s/2$ , and taking into account the change in the Moon-Earth direction, we obtain (Ivashkin 2002, 2003, 2004a):

$$\Delta E_S \approx \text{sign}\beta \left( \frac{15}{2} \pi \mu_E \left( \frac{\mu_M}{a_M} \right)^3 n_M \beta \right)^{2/9} > 0. \quad (2)$$

In Eqn. 2: value  $\mu_E$  is the Earth's gravitational parameter, value  $a_M$  is the semimajor axis of the Moon's orbit, value  $n_M$  is the angular velocity of its orbital motion,

$$\beta = \cos^2 \gamma \sin 2\alpha, \quad (3)$$

here angle  $\gamma$  is the slope of the radius vector  $r_B$  for an external body (for the Earth, in this case) to the plane of the particle orbit, and  $\alpha$  is the angle between the projection of the radius vector  $r_B$  onto this plane and the direction to the orbit perilune. For  $\Delta E_S > 0$ , it is necessary to have  $\sin 2\alpha > 0$ ,  $0 < \alpha < \pi/2$  or  $\pi < \alpha < 3\pi/2$ . Estimation by Eqns 2-3 gives  $\Delta E_S = -E_{s0} \approx 0.096 \text{ km}^2 \text{ s}^{-2}$ ,  $a_0 \approx 25,600 \text{ km}$  for middle value  $\beta = 0.5$ . This gives estimation for minimal value of semimajor axis  $a_0$  for the initial elliptic selenocentric orbit in the Moon-to-Earth detour trajectory. This theoretical evaluation well fits the results for our numerical calculations of the Moon-to-Earth detour trajectories. E.g., for the Moon-to-Earth flight during a month from May 12, 2001, and for initial inclination  $i_0 = 90^\circ$ , we received for the Moon-to-Earth calculated trajectories the minimal value of semimajor axis  $a_{0min} \approx 24,500\text{-}27,000 \text{ km}$  for initial ascending node  $\Omega_0 = 0$ ;  $a_{0min} \approx 23,500\text{-}28,500 \text{ km}$  for  $\Omega_0 \approx -63.9^\circ$ ;  $a_{0min} \approx 24,000\text{-}28,000 \text{ km}$  for  $\Omega_0 = -90^\circ$ , see Figure 5.

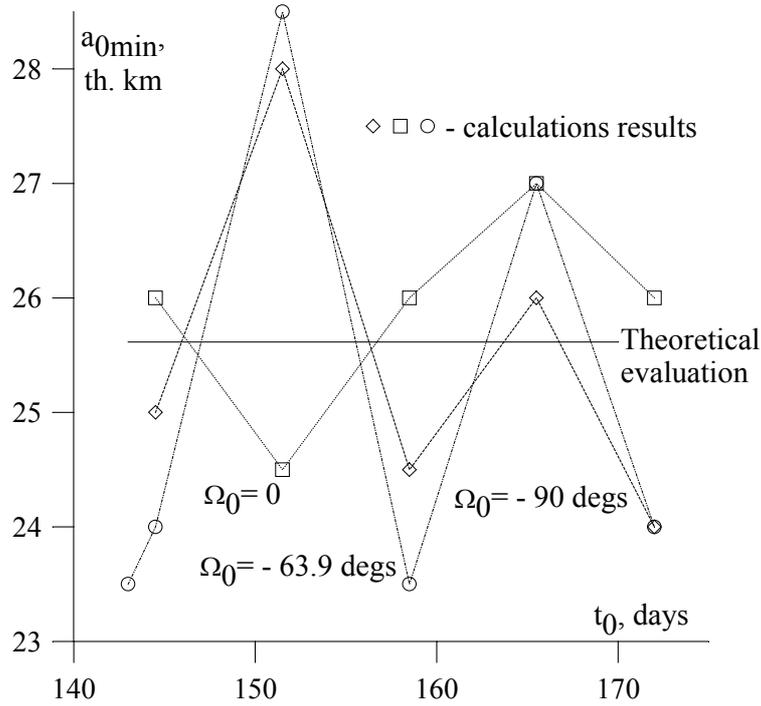


Figure 5. Minimal value of initial semimajor axis depending on the time of start from near-Moon elliptic selenocentric orbit for the Moon-to-Earth detour trajectories.

We can see that, if the orientation of the particle initial orbit relative to the Earth is suitable and its negative energy is large enough, the Earth's gravitation provides a sufficient increase in the particle orbital energy and allows its passive escape from the lunar attraction.

#### 4. Earth's gravity effect on the particle acceleration to hyperbolic selenocentric motion

Now we approximately analyze the acceleration of the particle motion with respect to the Moon from the zero energy to a positive one for a hyperbolic trajectory with velocity at "infinity"  $V_\infty$  which is equal to about 0.15 – 0.25 km/s on the subsequent short arc  $E_s P_2 P_3$  (even on the somewhat larger arc  $P_1 E_s P_2 P_3$  from the energy  $E_s < 0$ ). This acceleration is qualitatively described by approximate model of the one-dimensional rectilinear particle's motion with the Earth, placed on the same line at a distance  $r_M$  beyond the Moon (Ivashkin 2002, 2003, 2004a), see Figure 6.

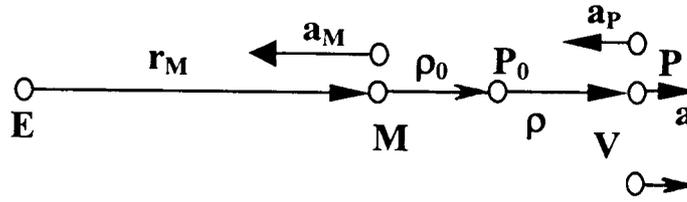


Figure 6. A model for the particle selenocentric motion from the Moon.

In this case  $d\rho/dt > 0$ , i.e., the particle moves away from the Moon. The Earth's perturbation  $\delta a_E = \mu_E/r_M^2 - \mu_E/(r_M + \rho)^2 > 0$ , it accelerates the particle motion. For this model, assuming that, approximately,  $r_M = \text{const}$ , we can integrate the equations for the perturbed motion of the particle:

$$V^2(\rho) = 2E_s(\rho) + 2\mu_M / \rho; \quad (4)$$

$$t(\rho) - t_0 = \int_{\rho_0}^{\rho} d\rho / V(\rho); \quad (5)$$

$$E_s(\rho) - E_0 = (\mu_E / r_M^2)(\rho - \rho_0) + \mu_E / (r_M + \rho) - \mu_E / (r_M + \rho_0), \quad E_s(\rho_0) = E_0; \quad (6)$$

inversely:

$$\rho(E_s) = B/2 + [B^2/4 + r_M B]^{1/2}; \quad (7)$$

where

$$B = (E_s - E_0)r_M^2 / \mu_E + \rho_0^2 / (r_M + \rho_0). \quad (8)$$

**Example.** Let for the presented trajectory at the point Es of the gravitational escape the selenocentric energy be  $E_s = E_0 = 0$ ,  $\rho = \rho_0 = 91850$  km,  $r_M = 376000$  km. Then, the model of Eqns. 4-8 gives  $\rho \approx 102.5 \cdot 10^3$  km for  $V_\infty = 0.15$  km/s (point P<sub>2</sub>),  $\rho \approx 120.4 \cdot 10^3$  km for  $V_\infty = 0.25$  km/s (point P<sub>3</sub>), and  $\rho \approx 55 \cdot 10^3$  km for  $E_s = -0.031$  km<sup>2</sup>/s<sup>2</sup> (point P<sub>1</sub>). We can see the qualitative correspondence with the numerical results presented above, especially for  $E_s > 0$ .

Thus, for the given class of the Moon-to-Earth detour space flights, the Earth's gravitation in the region of the translunar libration point L<sub>2</sub> allows increasing the selenocentric energy of the particle motion from the zero value to the positive one for a hyperbolic trajectory. If the selenocentric hyperbolic velocity  $V_\infty$  of the particle is directed along the Moon velocity, the geocentric energy and the apogee distance will be increased and the particle runs away from the Moon orbit and from the Earth, at a large geocentric distance.

## 5. Sun's gravity effect on decrease of the particle orbit perigee distance

Next, we estimate the effect of the Sun gravitation on the variation  $\Delta r_\pi$  of the particle orbit perigee distance  $r_\pi$  on the final arc P<sub>3</sub> F of the space flight. We use the theory (Lidov 1961, 1962) of the orbit evolution for one orbital revolution of a planet's (the Earth', here) satellite due to an external body's (the Sun's, now) gravity perturbation assuming the Earth-Sun direction to be constant. Since the final geocentric distance  $r_{\pi f}$  for the particle orbit perigee is very small ( $r_{\pi f} = r_{\pi 0} + \Delta r_\pi \approx 0$ ), we assume that eccentricity  $e \approx 1$  and take for  $r_\pi$  its mean value  $r_\pi = (2r_{\pi f} - \Delta r_\pi)/2 \approx -\Delta r_\pi/2$ . Thus, we have:

$$\Delta r_\pi \approx \text{sign}\beta \left( \frac{15}{2} \pi \frac{\mu_S}{\mu_E} \beta \right)^2 a^7 / a_E^6 < 0. \quad (9)$$

Here,  $\mu_S$  is the gravitational parameter of the Sun,  $a_E$  and  $a$  are the semimajor axes for the Earth's orbit and for the particle geocentric orbit, the value  $\beta$  is determined by Eqn. 3 with the Sun as the external body. For  $\Delta r_\pi < 0$ , it follows from Eqns. 9, 3 that  $\sin 2\alpha < 0$ ,  $\pi/2 < \alpha < \pi$  or  $3\pi/2 < \alpha < 2\pi$ . Then, we estimate the desired value of the semimajor axis for the spacecraft orbit as

$$a \approx [|\Delta r_\pi| a_E^6 / \left( \frac{15}{2} \pi \frac{\mu_S}{\mu_E} \beta \right)^2]^{1/7}. \quad (10)$$

For estimation, we have assumed that  $\Delta r_\pi = -500 \cdot 10^3$  km and  $\beta = -0.5$ . Then, according to Eqn. 10, the semimajor axis of the particle geocentric orbit at the final part of the flight is  $a \approx 870 \cdot 10^3$  km and its apogee distance is  $r_\alpha \approx 1500 \cdot 10^3$  km. If we take into account that the Earth-Sun direction is not constant in time, this changes the result only slightly. Thus, if the orientation of the particle orbit with regards to the Sun is suitable enough and the orbit apogee distance is large enough (of about  $1.5 \cdot 10^6$  km), the particle perigee distance decreases from about the lunar-orbit radius to almost zero. This allows the particle's passive approach the Earth.

## 6. Conclusions

Reviewing the results of our analysis, we can see that gravitational perturbations of the Earth and the Sun make it possible for the particle beginning its motion from the selenocentric elliptic orbit to escape the motion from the lunar attraction, to transfer it to the Moon-to-Earth detour trajectory, and then to approach the Earth. This leads to noticeable decrease in the energy consumption for the Moon-to-Earth space flights. Such a conclusion is confirmed by both the numerical calculations of relevant trajectories and their theoretical analysis.

## Acknowledgements

The author would like to emphasize that this study is the development of the previous analysis of the Earth-to-Moon space flight trajectories (Ivashkin 2002, 2003, 2004a), which was initiated and supported by the GMV SA (Madrid, Prof. J.J. Martínez Garcia, Dr. M. Belló Mora, Dr. E. Revilla Pedreira, Dr. M. Martínez, and L.A. Mayo Muñiz). The presentation is supported by the ICEUM-6 Organizing Committee, by the Keldysh Institute of Applied Mathematics (Moscow, Russia) and by the Russian Foundation for Basic Studies (Project No. 04-01-10797z).

## References

- Belbruno E A and Miller J K 1993 Sun-Perturbed Earth-to-Moon Transfer with Ballistic Capture; *Journal of Guidance, Control and Dynamics* **16** No. 4 pp. 770-775.
- Belló Mora M, Graziani F, et al. 2000 *A Systematic Analysis On Weak Stability Boundary Transfers To The Moon*: Presented at the 51st International Astronautical Congress, held in Rio de Janeiro, Brazil, October 2000. Paper IAF-00-A.6.03, 12 p.
- Egorov V A and Gusev L I 1980 *Dynamics of the Earth-to-Moon Space flights* (Moscow, USSR: Nauka Publishers).
- Gatland K 1982 *The Illustrated Encyclopedia of Space Technology* (London: Salamander Book Ltd.).
- Hiroshi Yamakawa, Jun'ichiro Kawaguchi, Nobuaki Ishii, Hiroki Matsuo 1993 *On Earth-Moon Transfer Trajectory with Gravitational Capture*: Presented at AAS/AIAA Astrodynamics Specialist Conference, Victoria, USA. Paper AAS 93-633, 20 p.
- Ivashkin V V 2002 On Trajectories of the Earth-Moon Flight of a Particle with its Temporary Capture by the Moon; *Doklady Physics, Mechanics* **47** No. 11 pp. 825-827.
- Ivashkin V V 2003 *On the Earth-to-Moon Trajectories with Temporary Capture of a Particle by the Moon*: Presented at the 54th International Astronautical Congress, held in Bremen, Germany, September 29 – October 3, 2003. Paper IAC-03-A.P.01 pp. 1-9.
- Ivashkin V V 2004a *On Trajectories for the Earth-to-Moon Flight with Capture by the Moon*; Proceedings of the International Lunar Conference 2003 / International Lunar Exploration Working Group 5 – ILC2003/ILEWG 5, held November 16-22, 2003 in Waikoloa Beach Marriott Hotel, Hawaii Island, USA. Eds: Steve M. Durst, et al. American Astronautical Society AAS. Vol. 108, Science and Technology Series. Published for the AAS and Space Age Publishing Company, Paper AAS 03-723 pp. 157-166.
- Ivashkin V V 2004b On Particle's Trajectories of Moon-to-Earth Space Flights with the Gravitational Escape from the Lunar Attraction; *Doklady Physics, Mechanics* **49** No. 9 pp. 539-542.

- Ivashkin V V 2004c *On the Moon-to-Earth Trajectories with Gravitational Escape from the Moon Attraction*: Presented at the 18<sup>th</sup> International Symposium of Space Flight Dynamics, held in Munich, Germany, 11-16 October, 2004. Paper P0111, <http://www.issfd.dlr.de/papers/P0111.pdf>.
- Koon W S, Lo M W, Marsden J E, et al. 2001 Low Energy Transfer to the Moon; *Celestial Mechanics and Dynamical Astronomy* (Kluwer Academic Publishers, Netherlands) **81** pp. 63-73.
- Lidov M L 1961 Evolution of the Planets Artificial Satellites Orbits under Effect of the Outer Bodies Gravity Perturbations; *Artificial Satellites of the Earth* (Moscow, USSR: Nauka Publishers) **8** pp. 5–45.
- Lidov M L 1962 The Evolution of Orbits of Artificial Satellites of Planets under the Action of Gravitational Perturbations of External Bodies; *Planet. Space Sci* (Pergamon Press Ltd. Printed in Northern Ireland) **9** pp.719-759.
- Stepan'yants V A and L'vov D V 2000 Effective Algorithm for the Motion Differential Equations System Solving; *Mathematical Modeling* (Moscow, Russia), **12** No. 6 pp. 9-14.
- Sternfeld A 1934 Sur les trajectoires permettant d'un corps attractit central à partir d'une orbite keplérienne donnée; *Comptes rendus de l'Acad. des Sciences* (Paris, France) **198** pp. 711-713.
- Sternfeld A 1937 *Introduction to Cosmonautics* (Moscow, USSR: ONTI NKTP Publishers). 1974 the 2<sup>nd</sup> edition (Moscow, USSR: Nauka Publishers).
- Sternfeld A 1956 *Artificial Satellites of the Earth* (Moscow, USSR: GITTL Publishers). 1956 the 2<sup>nd</sup> edition *Artificial Satellites* (Moscow, USSR: GosTekhIzdat Publishers).